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# Room temperature multiferroism in CaTcO<sub>3</sub> by interface engineering

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# A R T I C L E I N F O

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# 1. Introduction

ABO<sub>3</sub> perovskite continues to prove itself to be an important family of multifunctional materials. This is because various instabilities can be simultaneously present within its simple cubic structure at high temperature [1–8]. Many of these instabilities such as magnetic, ferroelectric, antiferrodistortive, and antiferroelectric orderings and their interactions are closely associated with different functionalities that are useful for the device applications [9]. Recently a lot of excitement has been generated, again, in  $ATcO_3$  (A = Ca, Sr, Ba) as a new family of perovskite [10–12]. Similar to its isovalent neighbor of Mn ( $4s^23d^5$ ), technetium has a  $5s^24d^5$ electronic configuration with a occupied  $t_{2g}$  and empty  $e_g$  bands according to the crystal field theory. ATcO<sub>3</sub> has the G-type antiferromagnetic (AFM) configuration experimentally [10,12]. Strikingly, ATcO<sub>3</sub> is discovered to have an anomalously high magnetic ordering temperature, e.g., the Neél temperature of CaTcO<sub>3</sub> is approximately 800 K [10–12], which adopts Pnma space group symmetry all the way below 1273 K [10]. This is in sharp contrast to that of manganese perovskite, in which CaMnO<sub>3</sub> only has a Neél temperature of 123 K [13,14].

Progress has already been made in understanding the electronic structures and the magnetic exchange properties in  $ATcO_3$  (A = Ca, Sr, Ba) [10–12]. However, the detailed studies of the structural instabilities and their interactions are not yet available in litera-

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# ABSTRACT

We carry out systematic studies of the structural instabilities of the new perovskite family  $ATcO_3$  (A = Ca, Sr, Ba) by first-principles calculations. The orthorhombic ground state of  $CaTcO_3$  and  $SrTcO_3$  are found to be closely related to structural distortions due to the zone boundary phonon instabilities. We also identify a weak ferroelectric instability in  $CaTcO_3$ , which is however suppressed at the ground state due to the large antiferrodistortive mode. We show that the ferroelectricity in  $CaTcO_3$  can be induced in the  $CaTcO_3/BaTcO_3$  superlattices. Two types of interface mechanisms are involved, one is realized by the mismatch of the antipolar modes between two parent bulk materials and the other is the suppression of antiferrodistortive mode at interface. The Néel temperature of  $CaTcO_3/BaTcO_3$  superlattices is found to be ~816 K, indicating that  $CaTcO_3$  can be engineered into a new room temperature multiferroic material.

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ture. More importantly, keeping this intriguingly high Neél temperature in mind, one might be wondering whether or not more functionalities could be explored in this new family of perovskite.

In this work, we first use the density functional theory (DFT) to perform a systematic investigation of the structural instabilities and distortions in  $ATcO_3$  (A = Ca, Sr, Ba). A variety of structural instabilities has been identified. At ground state of CaTcO<sub>3</sub> and SrTcO<sub>3</sub>, the antiferrodistortive (AFD) modes associated with oxygen octahedral rotations are found to originate from the zone boundary phonon instabilities at M and R points. An antipolar structure is found in CaTcO<sub>3</sub> and SrTcO<sub>3</sub> originating from the antiferroelectric instability at X point and a trilinear coupling with M and R instabilities that lowers the free energy. An ferroelectric (FE) instability is discovered in only CaTcO<sub>3</sub>, which is however suppressed by the large AFD mode at the ground state. In the second part, we theoretically investigate the interface induced ferroelectric polarization in CaTcO<sub>3</sub>/BaTcO<sub>3</sub> superlattice. By taking advantage of the intrinsic structural instabilities in CaTcO<sub>3</sub>, including antipolar and FE ones, we propose that the FE can be induced at the interfaces of the superlattice by two interface engineering approaches. First, the electric polarization can be induced by the mismatch of antipolar structure between BaTcO<sub>3</sub> and CaTcO<sub>3</sub>. Second, the large oxygen octahedral rotation will be suppressed at the interface which can be used to enhance the intrinsic FE mode [15-17]. This picture is confirmed by our DFT calculations and the analysis of CaTcO<sub>3</sub>/BaTcO<sub>3</sub> superlattices. Finally, the Neél temperature of the superlattice is calculated to be  $\sim$ 816 K by a following Monte Carlo simulation. Our theoretical predictions clearly suggest that





COMPUTATIONAL MATERALS SCIENCE the room temperature multiferroism can be achieved in CaTcO<sub>3</sub> by interface engineering.

The rest of the paper is organized as follows. Section 2 introduces the technical details of the calculation. Section 3 is devoted into the results and discussions of of in structural instabilities of prototype cubic phase and orthorhombic ground state of bulk  $ATcO_3$  (A = Ca, Sr, Ba), followed by describing the induced polarization in CaTcO<sub>3</sub>/BaTcO<sub>3</sub> superlattices. We summarize in Section 4.

#### 2. Computational methods

Our DFT calculations are done by using the VASP code package [18,19]. In particular, both hybrid functional within the Heyd–Scuseria–Ernzerhof (HSE) scheme [20] and the Perdew–Burke–Ernzerhof functional revised for solids (PBEsol) [21] within the generalized gradient approximation (GGA) are adopted to treat the exchange correlation for electrons. These DFT functionals are known to be very accurate in predicting the volume of solids which is particularly important because the FE instability is sensitive to the cell volume. A 500 eV planewave energy cutoff and  $6 \times 6 \times 4 k$  mesh points converge very well the results of bulk ATCO<sub>3</sub> (A = Ca, Sr, Ba). Ionic coordinates are considered to be fully relaxed until the Hellmann–Feynman force is less then 1 meV/Å. For the superlattices, we use a smaller mesh of  $6 \times 6 \times 2 k$  points samplings.

In our HSE hybrid functional calculations, a mixing parameter of a = 0.3 is adopted. The adoption of mixing parameter in HSE functional is chosen because its closeness in both effective magnetic moment and lattice constant to the experimental values [10,12]. In the calculation based on PBEsol functional, an on-site Coulomb interaction term U = 3.0 eV and exchange interaction J = 1 eV are used for technetium. Our criterion of choosing the effective on-site Coulomb interaction U - J is based on the matching of results in the lattice constant, band gap, and effective magnetic moment of Tc atoms to those calculated from the accurate HSE hybrid functional.

Our calculations on the cubic  $ATcO_3(A = Ba, Sr, Ca)$  is based on the  $Pm\bar{3}m$  space group symmetry in which the only degree of freedom that allowed to relax is the lattice constant *a*. In the cubic phase calculations, the main results are based on the GGA + U functional. In calculating the structural ground state of  $ATcO_3(A = Ba,$ Sr, Ca), both HSE and GGA + U functionals are used, where the symmetry is fixed at the experimentally identified Pnma space group.

In the calculations of BaTcO<sub>3</sub>/CaTcO<sub>3</sub> superlattices, HSE is only used for the 1BaTcO<sub>3</sub>/1CaTcO<sub>3</sub> short-period superlattice, whereas GGA + U is used in the other longer period superlattices. We carry out DFT calculations for BaTcO<sub>3</sub>/CaTcO<sub>3</sub> superlattices assuming the coherent growth on the substrate of GdScO<sub>3</sub> (a = 3.97 Å) [22] and NdScO<sub>3</sub> (a = 4.01 Å) [23]. The selections of substrates introduce small lattice mismatches by about  $\pm 1.26\%$  and  $\pm 2.7\%$  in BaTcO<sub>3</sub> and CaTcO<sub>3</sub> respectively, which are feasible for the experimental growth. The space group symmetry of BaTcO<sub>3</sub>/CaTcO<sub>3</sub> superlattices is found to be monoclinic (Pc). The ground state structure of superlattice is identified by systematically freezing all the structural instabilities found at cubic phase including octahedral rotations, antipolar, and ferroelectric modes into the supercell with high symmetry, in which a  $\sqrt{2}a \times \sqrt{2}a \times c$  is used. Then we perform the structural relaxation including both atomic positions and lattice constant along the superlattice growth direction. Finally, we have also carried out the phonon dispersion computation for the resulting superlattice structures and we found no leftover unstable mode.

To calculate the Neél temperature of the system, we perform Monte Carlo simulations [24] of a Heisenberg model on a  $12 \times 12 \times 12$  cubic cell with periodic boundary conditions. Each cubic cell contains four spins. We perform the simulations at temperatures ranging from 300 to 1300 K. At each temperature we carry out an initial 10,000 sweep to prepare the system, sample averages are accumulated over 750,000 sweeps.

### 3. Results and discussion

#### 3.1. Prototype cubic perovskite structures

In perovskite, the structural instabilities of the prototype cubic phase very often give valuable insights in understanding its low temperature structures and help to analyze its functional properties such as ferroelectricity and multiferroicity [25,26]. To this end, we first relax the structural parameters at cubic phase for ATcO<sub>3</sub> (A = Ca, Sr, Ba). In particular, the structural relaxations are performed based on several hypothetical spin configurations, which are G, A, C type antiferromagtic and ferromagnetic spin configurations respectively. The results are presented in Table 1.

It can be seen that for all the ATCO<sub>3</sub> under study, the G-type AFM configuration has the lowest total energy. This is also consistent with the G-type AFM magnetic configuration identified experimentally in CaTcO<sub>3</sub> and SrTcO<sub>3</sub> at room temperature [10,12]. Furthermore, The above results by GGA + U functional are checked by the more accurate HSE hybrid functional. As shown in Table 1, the results obtained from two functionals are quantitatively very close. In particular, both GGA + U and HSE accurately predict the lattice constant of cubic SrTcO<sub>3</sub> at 3.967 and 3.948 respectively. In comparison, the experimental value is 3.961 [27].

In Table 2, we present the Born effective charges ( $Z^*$ ) and the dielectric constant ( $\epsilon_{\infty}$ ) for cubic perovskite CaTcO<sub>3</sub>, SrTcO<sub>3</sub>, and BaTcO<sub>3</sub>. The effective charges on the A site and B site are isotropic; the effective charges of the oxygen atoms can be divided into two independent values,  $Z_{0\parallel}^*$  and  $Z_{0\perp}^*$ , which represent the dynamic charge transfer by perturbing the oxygen atom atom along the O-Tc bond direction and perpendicular to it respectively. Similar to other ABO<sub>3</sub> perovskites, we observe anomalously large  $Z_{0\parallel}^*$  resulting from the hybridization between oxygen 2p and Tc 4d electrons. However, the values are smaller than those in ATiO<sub>3</sub> and AMnO<sub>3</sub> with 3d electrons [28]. This is consistent with the trend

Table 1

Computed cubic ATcO<sub>3</sub> (A = Ca, Sr, Ba) structural parameters (Å) and total energy (eV) for different spin configurations with  $Pm\bar{3}m$  symmetry. The total energies of G-type AFM structures are chosen to be the references.

		CaTcO <sub>3</sub>	SrTcO <sub>3</sub>	BaTcO <sub>3</sub>
G-AFM	a <sub>0</sub> (Å)	3.904	3.967	4.036
	a <sub>0</sub> (Å)(HSE)	3.906	3.948	4.022
	Energy (eV)	0.000	0.000	0.000
A-AFM	a <sub>0</sub> (Å)	3.913	3.975	4.049
	Energy (eV)	1.065	1.038	0.998
C-AFM	a <sub>0</sub> (Å)	3.908	3.970	4.035
	Energy (eV)	0.449	0.448	0.443
FM	a <sub>0</sub> (Å)	3.917	3.976	4.048
	Energy (eV)	1.842	1.748	1.637

Table 2

Dielectric constants and Born effective charges (e) of cubic ATcO<sub>3</sub> (A = Ca, Sr, Ba) calculated by GGA + U functional. The structures are taken from from results by GGA + U functional in Table 1.

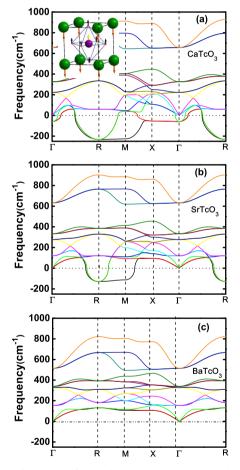
	CaTcO <sub>3</sub>	SrTcO <sub>3</sub>	BaTcO <sub>3</sub>
$Z^*_A$	2.69	2.66	2.87
$Z^*_{Tc}$	5.87	5.96	6.19
$Z^*_{0\parallel}$	-5.32	-5.38	-5.61
$Z^*_{\Omega^{\perp}}$	-1.62	-1.62	-1.72
$\epsilon_{\infty}$	8.64	8.60	9.14

of decreasing dynamic charges of B site atoms with 4*d* electrons in perovskite [26].

#### 3.2. Structural instabilities at cubic phase

In Fig. 1, we report the phonon dispersion curves of the cubic  $ATcO_3$  (A = Ca, Sr, Ba) along the high symmetry lines of the Brillouin zone. The lowest phonon frequencies at the high symmetry points ( $\Gamma$ , X, M, R) points are also listed in Table 3. In order to check the results by GGA + U, we also report the phonon frequencies by HSE hybrid functional in Table 3. It can be seen that, GGA + U does give qualitatively consistent features compared to those computed from HSE functional [29].

Compared to the structural instabilities in  $SrTcO_3$  and  $CaTcO_3$ , all phonon modes in  $BaTcO_3$  are stable. Obviously, in both  $SrTcO_3$  and  $CaTcO_3$ , the largest unstable phonons are  $M_3^+$  and  $R_5^-$  modes, which can be identified by the largest imaginary frequencies



**Fig. 1.** Phonon dispersions of the cubic  $ATcO_3$  (A = Ca, Sr, Ba) along the high-symmetry points, which are computed by GGA + U functional.

#### Table 3

Computed lowest phonon frequencies  $(cm^{-1})$  of cubic ATcO<sub>3</sub> (A = Ca, Sr, Ba) by HSE nybrid functional.

Approach	Material	$\Gamma_4^-$	$R_5^-$	$M_3^+$	$X_5^-$
HSE	CaTcO₃	58.28 <i>i</i>	232.39 <i>i</i>	232.46 <i>i</i>	53.34 <i>i</i>
	SrTcO₃	118.50	127.81 <i>i</i>	109.73 <i>i</i>	94.45
	BaTcO₃	151.51	130.44	106.39	103.41
GGA + U	CaTcO₃	88.06 <i>i</i>	221.82 <i>i</i>	216.48i	81.39 <i>i</i>
	SrTcO₃	134.09	152.11 <i>i</i>	137.43i	119.42
	BaTcO₃	214.82	141.43	167.12	141.43

around 200i cm<sup>-1</sup>. These large *R* and *M* points unstable modes suggest a strong tendency of out-of-phase and in-phase antiferrodistortive (AFD) oxygen octahedral rotation respectively.

The structural distortions due to the  $M_3^+$  and  $R_5^+$  instabilities will be discussed in the next subsection. They give rise to the experimentally identified orthorhombic ground state of Pnma space group symmetry. Besides the AFD instabilities, interestingly, a structural instability  $X_5^-$  is also identified at Brillouin zone boundary point (X) in CaTcO<sub>3</sub>.  $X_5^-$  mode in CaTcO<sub>3</sub> has a smaller imaginary frequency at 53*i* cm<sup>-1</sup>. The  $X_5^-$  mode is an antipolar structural instability and its eigenvector can be described by the Ca and O atoms move in the opposite directions in the CaO layers. The  $X_5^$ structural distortion is also developed at Pnma ground state in CaTcO<sub>3</sub> and SrTcO<sub>3</sub>, which will also be discussed in the next subsection.

However,  $CaTcO_3$  exhibits another weak unstable phonon mode  $\Gamma_4^-$  at Brillouin zone center. The  $\Gamma_4^-$  mode is a polar phonon mode, which may generate the electric polarization. The eigenvector of  $\Gamma_4^-$  phonon is depicted in the insert of Fig. 1(a), which can be described by the relative displacement of oxygen octahedral cage and the Ca atom. This particular pattern of ferroelectric phonon instability is refered as the *last* mode in literature [30].

This weak FE instability only exists in CaTcO<sub>3</sub> and is absent in either BaTcO<sub>3</sub> or SrTcO<sub>3</sub>. It is well-known that in the conventional perovskite  $ATiO_3$  (A = Ba, Sr, Ca), the cubic  $BaTiO_3$  has the strongest FE instability and the largest spontaneous polarization at low temperature tetragonal and rhombohedral phases [31]. On the other hand, cubic CaTiO<sub>3</sub> has the weakest FE polarization and stays as a paraelectric material at ground state. However, this can be understood by Goldschmidt criterion in terms of the so-called tolerance factor  $t = \frac{r_A + r_0}{\sqrt{2}(r_B + r_0)}$  [32]. For comparison, we present the tolerance factor for  $ABO_3$  families with B = Ti, Mn, and Tc respectively in Table 4. According to the Goldsmiths criterion, when t = 1, the perovskite prefers the idea cubic structure; when t > 1 it prefers the B-site driven ferroelectricity; when t < 1 the perovskite prefers both the A-site driven ferroeletricity and oxygen octahedral rotation at the same time. Because the radius of Tc is larger than that of Ti, the tolerance factor in BaTcO<sub>3</sub> is very close to 1 favoring the idea cubic structure; on the other hand, the tolerance factor of BaTiO<sub>3</sub> is larger than 1 favoring the B-site driven ferroelectricity. This is consistent with the absence of any structural instability in BaTcO<sub>3</sub>.

Similar weak FE instabilities are also found in other perovskite materials, such as CaMnO<sub>3</sub> [33] and CaTiO<sub>3</sub> [34]. However, the electric polarization is not able to develop in these materials because they are suppressed by the large oxygen octahedral rotation AFD modes, which is in strong competition with FE modes. In Section 3.4, we will discuss how to induce the FE by interface engineering method in superlattices.

#### 3.3. Pnma ground state

In experiments, the only available low symmetry structures found in CaTcO<sub>3</sub> and SrTcO<sub>3</sub> are the orthorhombic structures with Pnma space group symmetry [10,12]. The structural distortions from cubic to orthorhombic phase can be viewed as the combined condensations of the  $R_5^-$  and  $M_3^+$  zone boundary unstable phonon modes. As a result, in the Pnma structure, the oxygen octahedral exhibits out-of-phase rotation around [110] axis and in-phase oxygen rotation around [001] axis. In Glazer notation [35], they are referred to as  $a^-a^-c^0$  and  $a^0a^0c^+$  type oxygen rotations respectively. Following the convention in literature [36], we refer the oxygen octahedral rotation around [001] axis as *tilting* in the following paragraphs.

# Table 4 Computed tolerance factors (t) of typical perovskite-type oxides ABO<sub>3</sub> (with A = Ba, Sr, Ca and B = Ti, Mn, Tc).

t	CaTcO <sub>3</sub>	SrTcO <sub>3</sub>	BaTcO <sub>3</sub>
	0.914	0.947	1.004
t	CaTiO₃	SrTiO <sub>3</sub>	BaTiO₃
	0.966	1.002	1.062
t	CaMnO <sub>3</sub>	SrMnO₃	BaMnO <sub>3</sub>
	0.959	0.994	1.054

In Table 5, we present the relaxed orthorhombic structure of  $ATcO_3$  (A = Ba, Sr, Ca) with Pnma space group symmetry, in which the available experimental structures are also presented for comparison. It can be seen that the HSE hybrid functional accurately reproduces the experimental structures. On the other hand, the PBEsol functional slightly overestimates the lattice constants and volumes, which are typical for the GGA approximation of exchange correlation functionals.

It is worth to note that with the increasing radius of A site atoms, the rotational and tilting angles are decreasing from very large angle in CaTcO<sub>3</sub> to almost zero in BaTcO<sub>3</sub> as shown in Table 5. At the same time, the crystal structures also change from being strongly orthorhombic in CaTcO<sub>3</sub> to being cubic symmetry in BaTcO<sub>3</sub>. Indeed, the above trend is consistent with the Goldschmidt criterion in terms of the increasing structural factors as we have discussed in the previous subsection.

Except for the zone boundary  $R_5^-$  and  $M_3^+$  structural modes that generate the Pnma ground state structure, it is also interesting to note that the other less unstable structural instability,  $X_5^-$ , is also condensed in orthorhombic CaTcO<sub>3</sub> and SrTcO<sub>3</sub> generating the antipolar structure. This induced antipolar structure can be understood by the trilinear coupling term ~  $\lambda Q_{R_5} Q_{M_5^+} Q_{X_5^-}$  in the free energy phenomenologically [37,38]. As shown in Fig. 2(a), when only  $X_5^-$  structural distortion is frozen into the CaTcO<sub>3</sub>, the total energy starts with a shallow double-well potential. This is consistent with the weak  $X_5^$ phonon instability as discussed in previous subsection. However, when both  $R_5^-$  and  $M_3^+$  structural distortions are present, the resulting energy is much lower. The resulting single-well potential profile indicates that the antipolar structure is induced improperly by the trilinear coupling in the free energy term, as shown in Fig. 2(d).

Unfortunately, the FE structural instability at cubic phase although has similar imaginary frequency to  $X_5^-$ , is not condensed at Pnma ground state. This is due to the strong competition between FE and oxygen octahedral rotation [15,39]. In the end, we have recalculated the phonon dispersion for all the ATcO<sub>3</sub> materials in the orthorhombic phase and no unstable mode is found any more indicating that the we have found the ground state structures theoretically.

# 3.4. Induced ferroelectricity by interface design in proposed BaTcO $_3$ / CaTcO $_3$ superlattice

In this subsection, we focus on the discussion of the induced FE in CaTcO<sub>3</sub> by possible material engineering methods. In particular,

we are going to take advantage of two intrinsic structural instabilities in cubic CaTcO<sub>3</sub>, i.e.  $X_5^-$  and  $\Gamma_4^-$ , which are antipolar and polar modes respectively. The antipolar structural distortion is present at the orthorhombic ground state, while the polar one is not due to the large AFD octahedral rotations. With the intriguingly high Neél temperature found in CaTcO<sub>3</sub>, it is particularly desirable that the FE polarization could be recovered and turned into a new room temperature multiferroic material.

The above can be achieved in the artificial materials based on modern thin-film technology. In general, there are two approaches, which are the *epitaxial strain* and *interface engineering* methods respectively. We first try the epitaxial strain method. By using the coupling between polar instability and epitaxial strain applied by the substrate, the epitaxial strain has been very often used to induce the FE in other perovskite materials [40]. To do so, we apply both tensile and compressive strain on the cubic CaTcO<sub>3</sub> systematically in the range of  $\pm \sim 5\%$ . At the same time, we lower the space group symmetry in the calculations to allow the development of polarization along both *c* axis and in the *ab* plane. Unfortunately, our calculations show that CaTcO<sub>3</sub> persists to be paraelectric even as much as  $\pm 5\%$  has been applied.

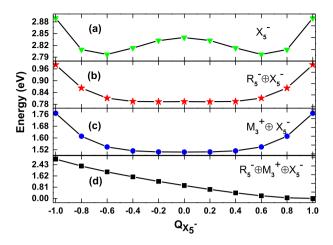
We then focus on the possibility of interface engineering. Compared with epitaxial strain, more dramatic changes in the strengths of instabilities can be achieved at the interfaces resulting in an overall change of functionalities [15–17,41]. We propose that the FE can be induced by the interfaces of the CaTcO<sub>3</sub>/BaTcO<sub>3</sub> superlattices. In particular, two types of interface engineering mechanisms are expected to take place that have been demonstrated recently in the literature [15,42]. First, FE can be induced by the mismatch of antipolar instabilities of two parent Pnma perovskites. This mismatch brings out a finite polarization at the interface due to the non-varnishing cancellation of antipolar moment. In literature, this is the so-called improper induced FE, because the antipolar in bulk is induced by the other two structural distortions  $R_5^-$  and  $M_3^+$ according to the trilinear coupling term  $\sim \lambda Q_{R_5^-} Q_{M_3^+} Q_{X_5^-}$  in free energy as discussed in the previous subsection [37,38]. With a large antipolar structural distortion in CaTcO<sub>3</sub> and an almost cubic BaTcO<sub>3</sub>, it can be expected that the electric dipole moment can be maximized at the interface of CaTcO<sub>3</sub>/BaTcO<sub>3</sub> superlattices. Secondly, it has been recently shown that a substantial reduction of AFD associated with octahedral rotations at the interface layer of CaTiO<sub>3</sub>/BaTiO<sub>3</sub> can be used to enhance the FE [15]. This is the socalled induced proper FE since it originates from the softening of intrinsic polar instability, e.g.  $\Gamma_4^-$  in cubic perovskite. Based on the same reasoning, we expect that the similar reduction of AFD mode will occur at the interface of CaTcO<sub>3</sub>/BaTcO<sub>3</sub>, which will further enhance the polarization. As a result, it will be very interesting to check if FE can be induced in the CaTcO<sub>3</sub>/BaTcO<sub>3</sub> short-period superlattices by the above comprehensive interface engineering mechanisms.

We assume the coherent growth of BaTcO<sub>3</sub>/CaTcO<sub>3</sub> superlattices on the substrate of GdScO<sub>3</sub> as schematically shown in Fig. 3. The first principles' results are summarized in Table 6. As one of the key results, the 1BaTcO<sub>3</sub>/1CaTcO<sub>3</sub> superlattice does exhibit a FE ordering with a spontaneous polarization  $P_s = 5.92 \,\mu c/cm^2$  by HSE func-

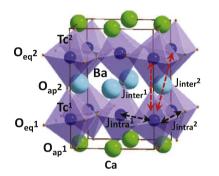
Table 5

Theoretically computed structural parameters, magnetic exchange angles (°) [11], oxygen octahedral rotation angles  $\phi_r(^\circ)$ , and tilting angles  $\phi_t(^\circ)$  of ground state ATcO<sub>3</sub> (A = Ca, Sr, Ba) with Pnma symmetry. The available experimental values [11] are also shown in parenthesis.

		a(Å)	b(Å)	c(Å)	$V(Å^3)$	$Tc - \widehat{O_1} - Tc$	$Tc - \widehat{O_2} - Tc$	$\phi_{ m r}$	$\phi_{\rm t}$
Pnma (HSE)	CaTcO <sub>3</sub>	5.53 (5.53)	7.71 (7.70)	5.39 (5.39)	230.05 (229.15)	150.90 (150.43)	150.91 (151.53)	10.04	14.55
	SrTcO <sub>3</sub>	5.56 (5.54)	7.86 (7.85)	5.61 (5.58)	244.92 (242.74)	163.39 (161.57)	167.76 (166.96)	0.60	8.32
	BaTcO <sub>3</sub>	5.69	8.05	5.67	260.20	179.96	179.90	0.049	0.019
Pnma (GGA + U)	CaTcO₃	5.57 (5.53)	7.73 (7.70)	5.41 (5.39)	232.08 (229.15)	148.41 (150.43)	148.91 (151.53)	10.63	15.80
	SrTcO₃	5.59 (5.54)	7.90 (7.85)	5.60 (5.58)	247.51 (242.74)	161.13 (161.57)	161.24 (166.96)	6.18	9.13
	BaTcO₃	5.71	8.08	5.71	262.87	179.94	179.88	0.058	0.032



**Fig. 2.** Energies profiles in CaTcO<sub>3</sub> as functions of mode amplitudes with frozen (a)  $Q_{X_{5}^{-}}$  only, (b) both  $Q_{R_{5}^{-}}$  and ground state mode amplitude of  $Q_{X_{5}^{-}}$ , (c) both  $Q_{X_{5}^{-}}$  and ground state mode amplitude of  $Q_{M_{3}^{+}}$ , (d)  $Q_{X_{5}^{-}}$ , and ground state mode amplitudes of  $Q_{R_{5}^{-}}$ ,  $Q_{M_{3}^{+}}$ . The normalization factor 1 is chosen by the mode amplitude (*Q*) at relaxed Pnma ground state in Table 5.



**Fig. 3.** Schematic atomic structure of relaxed 1CaTcO<sub>3</sub>/1BaTcO<sub>3</sub> superlattice at theoretical DFT ground state with monoclinic space group symmetry Pc.

tional (or similarly  $6.34 \,\mu\text{c/cm}^2$  by PBEsol functional) along the [110] in-plane axis. On the other hand, the pure CaTcO<sub>3</sub> grown on the same substrate does not exhibit any FE structural instability.

The emergence of FE ordering only in superlattice suggests that it is an interface effect. In order to further elucidate its interfacial origin, we employ the layer polarization decomposition to analyze the local polarization profile based on linear approximation [28] as shown in Table 6. In strained bulk CaTcO<sub>3</sub>, the local polarization profile is dominated by the clear antipolar ordering [42]. The relative displacement of Ca and O atom in the same plane generates a large dipole along [110] and  $[\bar{1}\bar{1}0]$  directions in alternate layers resulting a zero total polarization [42]. In superlattices, this large antipolar type local polarization  $\sim 27.6 \,\mu c/cm^2$  is preserved in the chemical environment, in which CaO is sandwiched by two TcO<sub>6</sub> octahedra. However, its magnitude is also perturbed at the interfaces as shown in Table 6. The local polarizations of CaO layer in 3:3 superlattice can be divided into two categories, bulk  $p_{\rm CTO}$  and interfaces of type I  $(p_{in}^{I})$ , which is defined by the local polarization of a CaO layer with one BaO layer as neighbor. One can see that the  $p_{\rm CTO}$  in 3:3 superlattice is almost the same value as that in strained bulk CaTcO<sub>3</sub>. The  $p_{in}^{l}$  is smaller than  $p_{b}$ , which is due to the suppressed oxygen rotations and tilting at the interface. In 2:2 superlattice, there is only one type of local polarization profile of CaO layer which belongs to interface type-I and  $p_{in}^{I}$  has a similar magnitude as that of 3:3 superlattice indicating the same chemical environment. However, in 1:1 superlattice, CaO layer is dominated by the type-II interfaces, in which the CaO layer is sandwiched by two BaO layers. This is in qualitatively difference with interface of longer period superlattices resulting in that  $p_{\rm in}^{\rm II} < p_{\rm in}^{\rm I}$ . A question arises: how we could understand the two different local polarization of interfacial CaO layers in one unified picture? We describe the interface effect on the local polarization by perturbation theory. It can be further assumed that the magnitude of perturbation is within the linear regime, in which  $p_{\rm in}^{\rm I}$  ( $p_{\rm in}^{\rm I}$ ) are only different from the bulk value by the perturbations introduced by the suppressed AFE ordering from one (two) neighboring BaO layers. Thus, one can arrive at  $p_{\rm in}^{\rm II} = p_{\rm CTO} - 2 \times (p_{\rm CTO} - p_{\rm in}^{\rm I}) \sim 19 \,\mu {\rm c/cm}^2$ . This is very close 19.38  $\mu {\rm c/cm}^2$  obtained from the actual DFT calculation.

The above local profile analysis clearly indicates that a large part of the interface induced FE is from the mismatch of antipolar distortion ( $X_5^-$  mode). The  $X_5^-$  phonon mode can be described as the atomic displacements along [110] direction including only the A site atoms and the apical oxygen atoms O<sub>ap</sub> in the same layer. However, the local analysis also shows that the AFD is largely suppressed at the interfaces. Therefore, a proper FE contribution can be also expected from the induced polarization. The proper FE originates from the zone center  $\Gamma_4^-$  in cubic perovskite and transforms into  $\Gamma_5^-$  with lower space group symmetry Pc in the supperlattices. The displacement of proper FE can be computed by the first-principles calculations in 1:1 superlattice with space group symmetry P4mm, in which the octahedral rotation and tilting are completely eliminated. As shown in Table 7, the proper FE mode displacement includes all the  $O_{ap}$ , equatorial oxygen  $O_{eq}$ , and A site atoms moving along [110] directions. Based on the modes's difference between improper and proper, we then performed the polarization mode decompositions into proper and improper contributions as shown in Table 7. Indeed, it can be seen that the improper polarization comprises the major part (78%) of the induced polarization, while the proper one contributes to the 22% rest of induced polarization. It can also be seen that the  $M_5^-$  and the  $M_3^+$  representing the  $a^0a^0c^$ and  $a^{-}a^{-}c^{0}$  type oxygen octahedral rotations do not have any contribution to induced polarization. This is consistent with the AFD nature of these oxygen rotations. The induced proper ferroelectricity is of particular interest. This is because it is associated with Tc ions, which are also responsible for the magnetism in these materials. Therefore, it is possible to achieve strong magnetoelectric coupling in the CaTcO<sub>3</sub>/BaTcO<sub>3</sub> short-period superlattices [16,17].

Interestingly, with both the proper and improper polarization at the interface, it is possible that the proper polarization can be further engineered by the epitaxial strain. In perovskite materials, such as SrTiO<sub>3</sub> and CaTiO<sub>3</sub>, the [110] in-plane polarization can be increased by applying tensile epitaxial strains. As shown in Table 7, we report the same mode decomposition of induced polarization for a larger tensile strain on NdScO<sub>3</sub> substrate. It can be seen that under this additional tensile strain, the displacement of equatorial oxygen  $O_{eq}$  is greatly increased. As a result, the induced proper polarization is also magnified by a factor of two. At the same time, we see a reduction of the improper contribution to the induced polarization. This is due to the smaller in oxygen octahedral rotation and tilting angles. It should be reminded that the effect of strain engineering is absent in bulk CaTcO<sub>3</sub>. This additional strain tunability of polarization further confirm that the interface induced polarization is of both proper and improper properties. Since the polarization of nBaTcO<sub>3</sub>/nCaTcO<sub>3</sub> is induced by interface, the maxium polarization is achieved in the shortest period superlattice, i.e. 1BaTcO<sub>3</sub>/1CaTcO<sub>3</sub>, in which the interfaces are the densest.

Both BaTcO<sub>3</sub> and CaTcO<sub>3</sub> have been found to have high Neél temperature well above room temperature. It has been argued that the more delocalized 4*d* orbital enhance the covalent hybridization with neighboring oxygen atoms, which in turn increase the hopping matrix according to the Anderson–Goodenough–Kanamori rules [10,44]. Therefore, it can be expected that the large magnetic

#### Table 6

Layer-by-layer decompositions of polarization  $p(\mu c/cm^2)$ , oxygen octahedral rotation angles  $\phi_r(^\circ)$ , and tilting angles  $\phi_r(^\circ)$  in the superlattices of 1BaTcO<sub>3</sub>/1CaTcO<sub>3</sub>(1:1), 2BaTcO<sub>3</sub>/ 2CaTcO<sub>3</sub>(2:2), 3BaTcO<sub>3</sub>/3CaTcO<sub>3</sub>(3:3), and strained bulk CaTcO<sub>3</sub> (CT<sup>s</sup>) and BaTcO<sub>3</sub>(BT<sup>s</sup>). The calculations are based on by GGA + U functional. The layer polarization is based on the definition centered on AO plane [43].

		$CaO_i^I$	TiO <sub>2</sub>	CaO <sub>b</sub>	TiO <sub>2</sub>	CaO <sup>I</sup>	TiO <sub>2</sub>	$BaO_i^I$	TiO <sub>2</sub>	$BaO_b$	TiO <sub>2</sub>	BaOl	TiO <sub>2</sub>
3:3													
	$p_{110}$	-23.11	-	27.58	-	-23.27	-	2.61	-	-0.33	-	2.72	-
	$p_{001}$	-5.85	-	-0.02	-	5.82	-	2.53	-	0.034	-	-2.48	-
	$\phi_{\rm r}$	-	9.34	-	9.20	-	6.38	-	-0.24	-	-0.33	-	6.14
	$\phi_{t}$	-	15.83	-	15.82	-	9.30	-	2.78	-	2.77	-	9.30
	$P_{110}^{\text{total}} =$	2.28				$P_{001}^{\text{total}} = 0.00$							
2:2													
	$p_{110}$	-22.10	-	-	-	23.39	-	-2.85	-	-	-	2.91	
	$p_{001}$	-5.55	-	-	-	5.57	-	2.73	-	-	-	-2.65	
	$\phi_{\rm r}$	-	9.76	-	-	-	5.79	-	-	-	0.46	-	5.77
	$\phi_{\rm t}$	-	14.62	-	-	-	9.51	-	-	-	4.38	-	9.50
	$P_{110}^{\text{total}} =$	0.068				$P_{001}^{\text{total}} = 0.00$							
		$CaO_i^{II}$	TiO <sub>2</sub>	BaO <sub>i</sub> <sup>II</sup>	TiO <sub>2</sub>								
1:1													
	<i>p</i> <sub>110</sub>	19.38	-	-6.12	-								
	$p_{001}$	0.02	-	0.04	-								
	$\phi_{\rm r}$	-	5.82	-	5.94								
	$\phi_{\rm t}$	-	9.41	-	9.41								
	$P_{110}^{\text{total}} =$	6.34				$P_{001}^{\text{total}} = 0.03$							
	110	CaO <sub>i</sub> II	-	-	BaO <sub>i</sub> II	-	-						
1:1 HSE		•											
	$p_{110}$	15.60	_	_	-4.39	_	_						
	$p_{001}$	0.04	_	-	0.08	_	-						
	$P_{110}^{\text{total}} =$					$P_{001}^{\text{total}} = 0.06$							
	1 110 -	-	CaO <sub>b</sub>	_	CaO <sub>b</sub>	- 0.00	_						
~~~S			cuob		Cuob								
CT <sup>S</sup>													
	<i>p</i> <sub>110</sub>	-	27.57	-	-27.58	-	-						
	$p_{001}$	-	0	-	0	-	-						
		-	$BaO_b$	-	BaO <sub>b</sub>	-	-						
BT <sup>S</sup>													
	$p_{110}$	-	0	-	0	-	-						
	$p_{001}$	-	0	-	0	-	-						

#### Table 7

The mode decomposition of the (CaTcO<sub>3</sub>)<sub>1</sub>/(BaTcO<sub>3</sub>)<sub>1</sub> superlattices of relaxed theoretical ground state with space group Pc grown on GdScO<sub>3</sub> and NdScO<sub>3</sub> substrates. The first-principles results are based on HSE hybrid functional.

	GdScO3 substrate (3.97 Å)						NdScO3 substrate (4.01 Å)				
	$\Gamma_5^-$ (total)	$\Gamma_5^-$ (proper)	$\Gamma_5^-$ (improper)	$M_5^-$	$M_3^+$	$\Gamma_5^-$ (total)	$\Gamma_5^-$ (proper)	$\Gamma_5^-$ (improper)	$M_5^-$	$M_3^+$	
Ca	0.2466	0.0393	0.2073	-	-	0.2520	0.0725	0.1795	-	-	
Ba	-0.0841	-0.0019	-0.0822	-	-	-0.0757	-0.0037	-0.0720	-	-	
Tc <sup>1</sup>	-0.0034	-0.0034	-	-	-	-0.0035	-0.0035	-	-	-	
Tc <sup>2</sup>	-0.0041	-0.0041	-	-	-	-0.0035	-0.0035	-	-	-	
O <sup>1</sup> <sub>ap</sub>	-0.1367	-0.0177	-0.1190	-	0.5487	-0.1380	-0.0301	-0.1079	-	0.5635	
$O_{ap}^{2}$	0.0018	0.0006	0.0012	-	0.2677	0.0042	0.0009	0.0033	-	0.2823	
O <sup>1</sup> <sub>eq</sub>	-0.0057	-0.0057	-	0.3486	0.4260	-0.0130	-0.0130	-	0.2772	0.4352	
0 <sup>2</sup> <sub>eq</sub>	-0.0072	-0.0072	-	0.3361	0.4270	-0.0123	-0.0123	-	0.2769	0.4357	
Q <sub>total</sub> (Å)	0.2944	0.0444	0.2527	0.4842	0.8582	0.2977	0.0807	0.2214	0.3918	0.8811	
$P(\mu C/cm^2)$	5.92	1.31	4.61	-	-	6.70	2.79	3.91	-	-	

antiferromagnetic coupling will be kept in the  $BaTcO_3/CaTcO_3$  superlattices. To further confirm this, we map the total energies in different magnetic configurations onto the Heisenberg Hamiltonian [4]

$$H = -\sum_{ii} J_{ij} S_i \cdot S_j. \tag{1}$$

The exchange coupling constants include the nearest-neighbor  $(J^1)$  and next -nearest-neighbor  $(J^2)$ , beyond which the coupling constant is found to be very small and could be neglected. This coupling constants are further decomposed into the contributions

from intralayer ( $J_{intra}$ ) and interlayers ( $J_{inter}$ ). The results are listed in Table 8. One can see that the exchange coupling constants are approximately the averages of those of the bulk BaTcO<sub>3</sub> and bulk CaTcO<sub>3</sub> in both intra- and inter- layer contributions. We obtain the AFM phase transition at 816 K from the Monte Carlo simulation. Furthermore, as explained in previous paragraphs, the mechanism of induced ferroelectric dipole moment is due to the noncancellation of anti-polar moments from CaTcO<sub>3</sub> and BaTcO<sub>3</sub> at the interface layer in the superlattices. The Pnma structural phase transition temperature in CaTcO<sub>3</sub> has been experimentally determined to be at 1273 K [10]. The structural phase transition in BaT-

#### Table 8

Effective magnetic moments  $m(\mu_B)$ , exchange coupling constants J(meV), and Neél temperature  $T_N(K)$  of bulk CaTcO<sub>3</sub>, bulk BaTcO<sub>3</sub>, and 1CaTcO<sub>3</sub>/1BaTcO<sub>3</sub> superlattice. GGA + U functional is used in the DFT calculations.

	CaTcO <sub>3</sub>	BaTcO <sub>3</sub>	1CaTcO <sub>3</sub> /1BaTcO <sub>3</sub>
т	2.14	2.09	2.05
$J_{inter}^1$	-38.10	-69.02	-52.60
$J_{intra}^1$	-38.10	-69.02	-60.29
$J_{inter}^2$	-0.78	-1.09	-2.89
$J_{intra}^2$	-0.78	-1.09	-3.17
T <sub>N</sub>	602	1089	816

 $cO_3$  has not been reported yet. This is consistent with our DFT results which show no unstable phonon mode, indicating  $BaTcO_3$  stays cubic structure at room temperature. Therefore, the above experimental and theoretical facts suggest that  $CaTcO_3/BaTcO_3$  should be multiferroic at room temperature.

## 4. Conclusion

Based on accurate first-principles calculations, we have performed careful studies of structural instabilities for the recently discovered perovskite  $ATCO_3$  (A = Ba, Sr, Ca). The experimental structures in  $CaTcO_3$  and  $SrTc_3$  are elucidated by the distortions originating from the structural instabilities and their couplings at prototype cubic phases. Based on the distinct structural instabilities in  $CaTcO_3$  and  $BaTcO_3$ , we propose and show that the electric polarization can be induced by the interfaces in  $BaTcO_3/CaTcO_3$ superlattices, in which comprehensive interface engineering mechanisms are taken into account. The theoretically proposed superlattice is found to be a new room-temperature multiferroic and await for future experimental confirmation.

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